

- 1 The diagram shows a right-angled triangle.

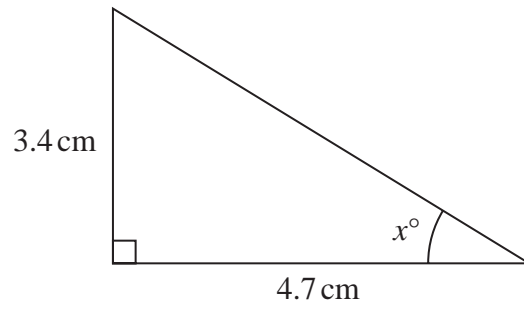


Diagram **NOT**
accurately drawn

Calculate the value of x .

Give your answer correct to one decimal place.

$$\tan x^\circ = \frac{3.4 \text{ cm}}{4.7 \text{ cm}} \quad (1)$$

$$x^\circ = \tan^{-1} \frac{3.4}{4.7} \quad (1)$$

$$= 35.9^\circ \quad (1)$$

$$x = 35.9$$

(Total for Question 1 is 3 marks)

2 The diagram shows cuboid $ABCDEFGH$.

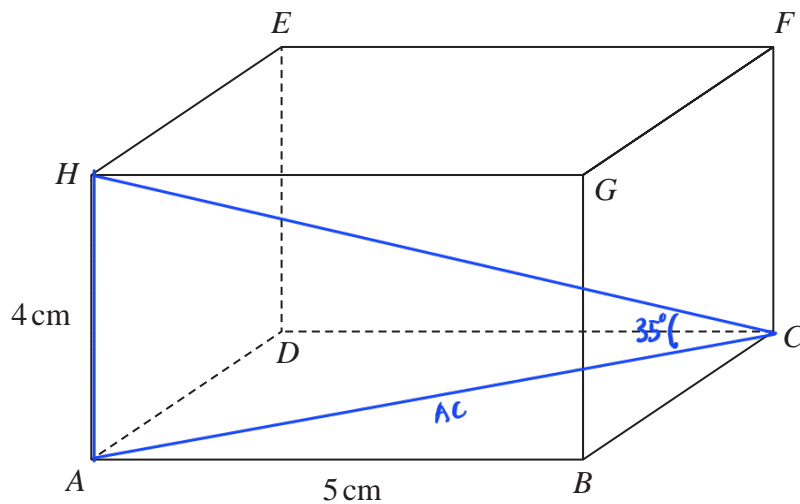


Diagram **NOT** accurately drawn

$$AB = 5 \text{ cm}$$

$$AH = 4 \text{ cm}$$

The size of the angle between CH and the plane $ABCD$ is 35°

Calculate the volume of the cuboid.

Give your answer correct to 3 significant figures.

① Find length BC

② Volume = $4 \times 5 \times BC$

$$\tan 35^\circ = \frac{4 \text{ cm}}{AC} \quad (1)$$

$$AC = \frac{4 \text{ cm}}{\tan 35^\circ}$$

$$= 5.71 \text{ cm} \quad (1)$$

$$AC^2 = AB^2 + BC^2$$

$$BC^2 = AC^2 - AB^2$$

$$BC^2 = 5.71^2 - 5^2$$

$$BC = \sqrt{5.71^2 - 5^2} \quad (1)$$

$$= 2.76 \dots$$

$$\text{Volume of cuboid} : 4 \times 5 \times 2.76 \quad (1)$$

$$= 55.3 \quad (1)$$

55.3

..... cm^3

(Total for Question 2 is 5 marks)

3 Here is a right-angled triangle.

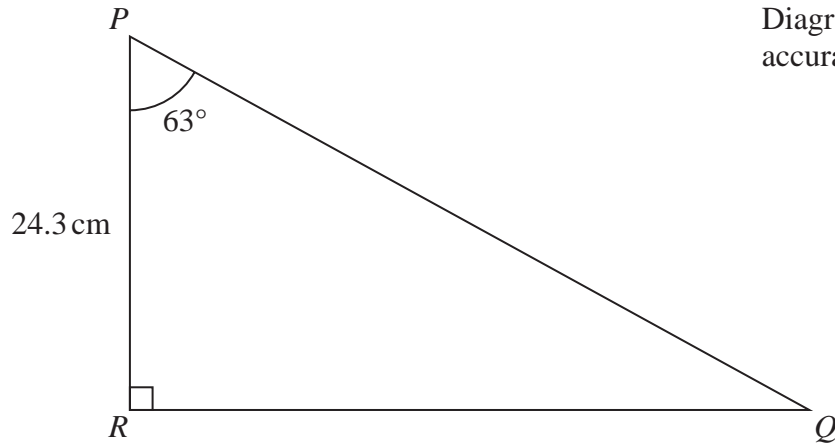


Diagram **NOT**
accurately drawn

Calculate the length of PQ .

Give your answer correct to 3 significant figures.

$$\cos 63^\circ = \frac{PR}{PQ}$$

$$\cos 63^\circ = \frac{24.3}{PQ} \quad (1)$$

$$PQ = \frac{24.3}{\cos 63^\circ} \quad (1)$$

$$= 53.5 \text{ cm} \quad (1)$$

53.5

..... cm

(Total for Question 3 is 3 marks)

- 4 The diagram shows two hot air balloons.

A is a point on the base of one of the balloons and B is a point on the base of the other balloon.

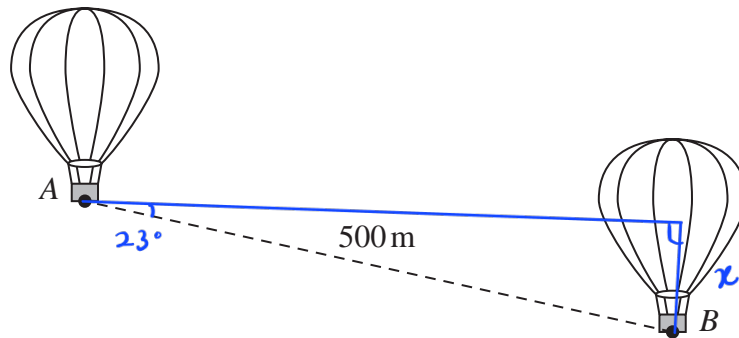


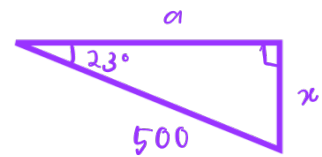
Diagram **NOT** accurately drawn

The distance between A and B is 500 metres.

The angle of depression of B from A is 23°

Calculate the vertical height of A above B .

Give your answer correct to one decimal place.



$$\sin \theta = \frac{o}{h}$$

$$\sin 23^\circ = \frac{x}{500} \quad (1)$$

$$x = 500 \sin 23^\circ \quad (1)$$

$$= 195.4 \text{ (1dp)} \quad (1)$$

195.4

metres

(Total for Question 4 is 3 marks)

5 Here is isosceles triangle ABC .

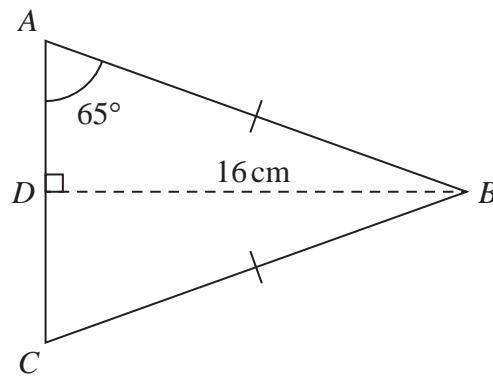


Diagram **NOT**
accurately drawn

D is the midpoint of AC and $DB = 16$ cm.

Angle $DAB = 65^\circ$

Work out the perimeter of triangle ABC .
Give your answer correct to one decimal place.

$$AD = \frac{16}{\tan 65^\circ} \quad (1)$$

$$= 7.4609 \dots \text{ cm}$$

$$AB = \frac{16}{\sin 65^\circ}$$

$$= 17.654 \dots \text{ cm} \quad (1)$$

$$\text{Perimeter} = 2(17.654 \dots) + 2(7.4609 \dots) \quad (1)$$

$$= 50.2 \text{ cm (1dp)} \quad (1)$$

..... 50.2 cm

(Total for Question 5 is 4 marks)

6 The diagram shows triangle ABP inside the regular hexagon $ABCDEF$

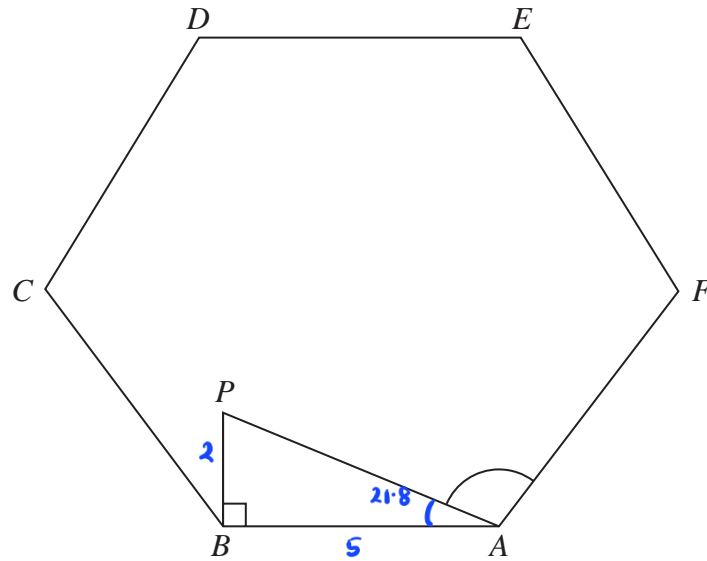


Diagram **NOT**
accurately drawn

$$AB = 5 \text{ cm}$$

$$BP = 2 \text{ cm}$$

$$\text{Angle } ABP = 90^\circ$$

Work out the size of angle PAF

Give your answer correct to 3 significant figures.

$$\begin{aligned} \text{Internal angle of hexagon} &= \frac{6-2}{6} \times 180^\circ \\ &= \frac{4}{6} \times 180^\circ \\ &= 120^\circ \quad (1) \end{aligned}$$

$$\tan BAP = \frac{2}{5} \quad (1)$$

$$\begin{aligned} BAP &= \tan^{-1} \frac{2}{5} \quad (1) \\ &= 21.8^\circ \end{aligned}$$

$$\begin{aligned} \text{angle } PAF &= 120^\circ - 21.8^\circ \quad (1) \\ &= 98.2^\circ \quad (1) \end{aligned}$$

98.2

(Total for Question 6 is 5 marks)

- 7 The diagram shows triangle PQR .

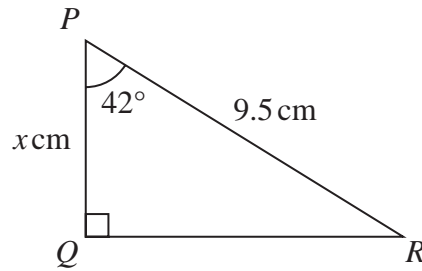


Diagram **NOT**
accurately drawn

Work out the value of x
Give your answer correct to one decimal place.

$$\cos 42^\circ = \frac{x}{9.5} \quad (1)$$

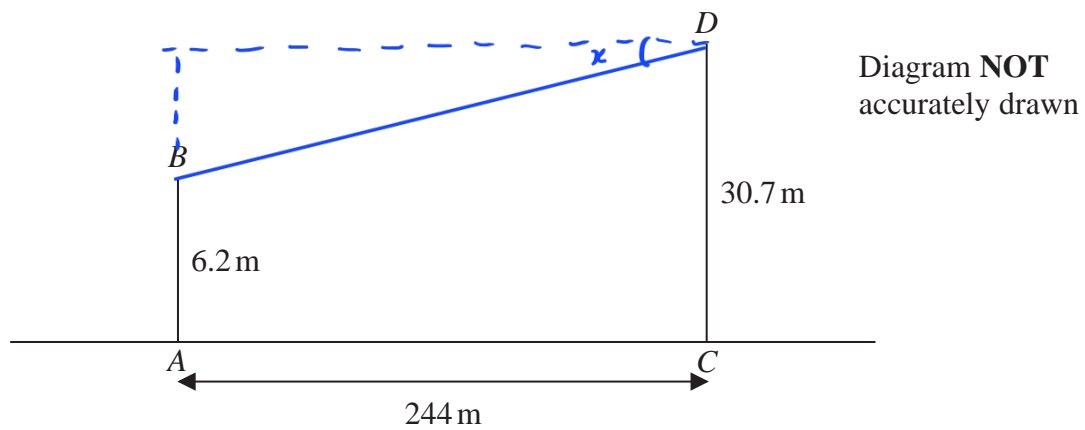
$$x = 9.5 \cos 42^\circ \quad (1)$$

$$= 7.1 \quad (1)$$

$$x = \dots\dots\dots 7.1$$

(Total for Question 7 is 3 marks)

- 8 The diagram shows two vertical phone masts, AB and CD , on horizontal ground.



$$AB = 6.2 \text{ m} \quad AC = 244 \text{ m} \quad CD = 30.7 \text{ m}$$

Work out the size of the angle of depression of B from D
Give your answer correct to one decimal place.

$$\tan x = \frac{30.7 - 6.2}{244} \quad (1)$$

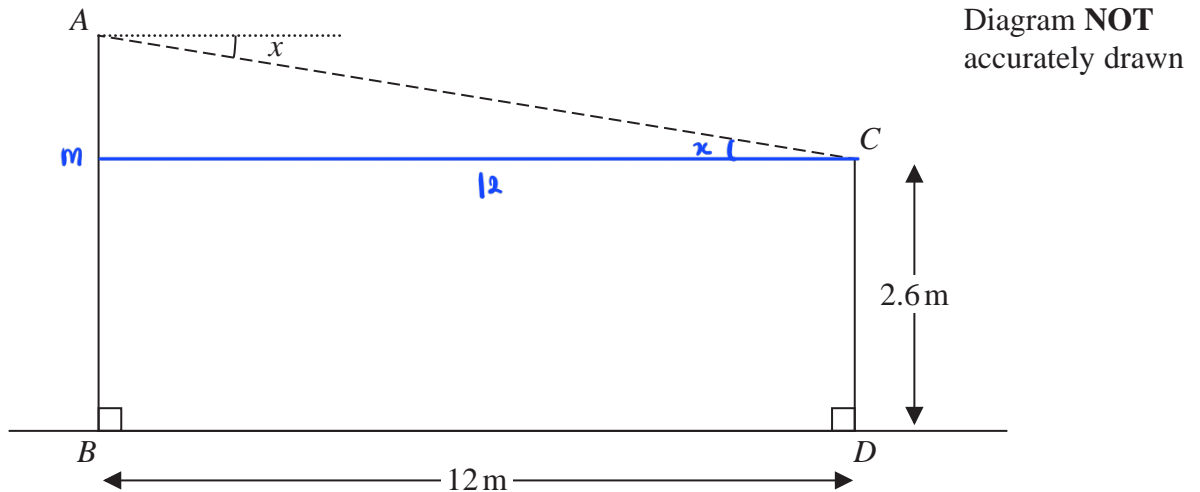
$$x = \tan^{-1} \frac{24.5}{244} \quad (1)$$

$$= 5.7 \quad (1)$$

5.7

(Total for Question 8 is 3 marks)

- 9 A zip wire is shown as the dashed line AC in the diagram.



The zip wire is supported by two vertical posts AB and CD standing on horizontal ground.

$$CD = 2.6 \text{ m} \quad BD = 12 \text{ m}$$

The zip wire makes an angle x with the horizontal, as shown in the diagram. The design of the zip wire requires the angle x to be at least 5°

Work out the least possible height of the post AB
Give your answer correct to 3 significant figures.

$$\tan 5 = \frac{Am}{12}$$

$$Am = 12 \tan 5 \quad (1)$$

$$= 1.05$$

$$AB = 2.6 + 1.05 \quad (1)$$

$$= 3.65 \quad (1)$$

3.65 m

(Total for Question 9 is 3 marks)

10 R and T are points on a circle, centre O

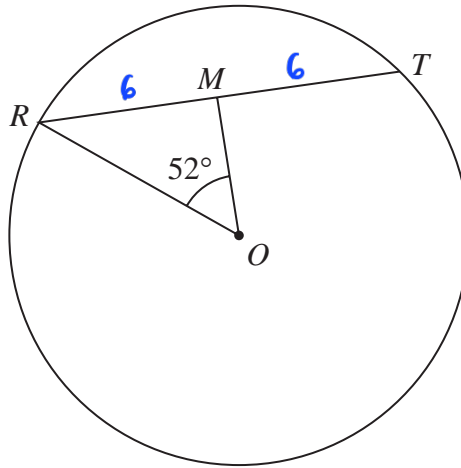


Diagram **NOT**
accurately drawn

$$RT = 12 \text{ cm}$$

M is the midpoint of RT

$$\text{Angle } ROM = 52^\circ$$

Work out the area of the circle.

Give your answer correct to 3 significant figures.

$$\sin 52^\circ = \frac{6}{r} \quad (1)$$

$$r = \frac{6}{\sin 52^\circ} \quad (1)$$

$$= 7.614$$

$$\text{Area} = \pi \times 7.614^2 \quad (1)$$

$$= 182 \quad (1)$$

182 cm^2

(Total for Question 10 is 4 marks)

- 11 The diagram shows a rectangular sheet of metal $ABCD$

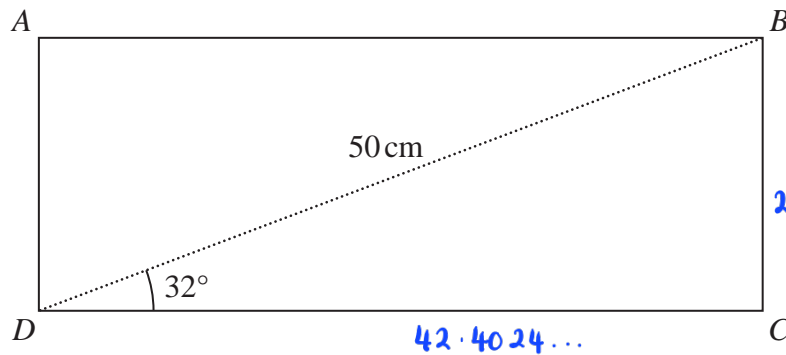


Diagram **NOT**
accurately drawn

$BD = 50$ cm and angle $BDC = 32^\circ$

Nasser joins side AD to side BC to form a cylinder.

BC is the height of the cylinder.

DC is the circumference of the cross section of the cylinder.

Work out the volume, in cm^3 , of the cylinder.

Give your answer correct to 3 significant figures.

$$\sin 32^\circ = \frac{BC}{50} \quad (1)$$

$$BC = 50 \sin 32^\circ = 26.4959... \quad (1)$$

$$\cos 32^\circ = \frac{CD}{50} \quad (1)$$

$$CD = 50 \cos 32^\circ = 42.4024...$$

$$42.4024... = 2\pi r$$

$$r = \frac{42.4024...}{2\pi} = 6.74855... \quad (1)$$

$$\text{Volume} = \pi \times 6.74855...^2 \times 26.4959... \quad (1)$$

$$= 3796 \quad (1)$$

3 790 cm³

(Total for Question 11 is 6 marks)

12 The diagram shows right-angled triangle ABD

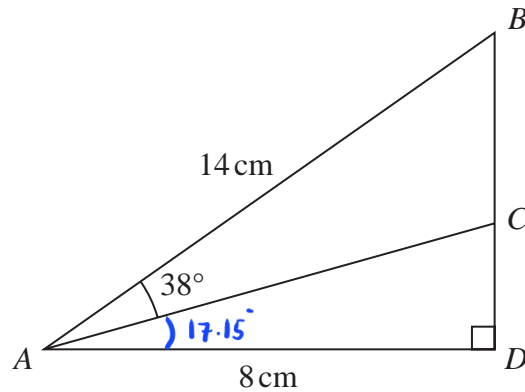


Diagram **NOT**
accurately drawn

$$AB = 14 \text{ cm} \quad AD = 8 \text{ cm}$$

C is the point on BD such that angle $BAC = 38^\circ$

Work out the length of CD

Give your answer correct to 3 significant figures.

$$\cos \angle BAD = \frac{8}{14} \quad (1)$$

$$\angle BAD = \cos^{-1} \frac{8}{14} = 55.15^\circ \dots \quad (1)$$

$$\angle CAD = 55.15^\circ - 38^\circ = 17.15^\circ$$

$$\tan 17.15^\circ = \frac{CD}{8} \quad (1)$$

$$\begin{aligned} CD &= 8 \tan 17.15^\circ \\ &= 2.47 \quad (1) \end{aligned}$$

2.47 cm

(Total for Question 12 is 4 marks)